Emmy Noether Looks at the Deconfined Quantum Critical Point

The deconfined quantum critical point (DQCP) describes a continuous phase transition between two phases that spontaneously breaks different symmetries [1]. Outside the realm of the Landau-Ginzburg-Wilson paradigm of phase transitions which is based on the concept of order parameter, the DQCP represents the new paradigm of quantum matter which manifests the concepts of fractionalized excitations (spinons in the model realization of the DQCP – the JQ model [2,3]) and emergent gauge structure and symmetry [4].

However, there still exist ambiguities in the presence of the emergent continuous symmetry at the DQCP. Up to now several numerical methods have been employed, including comparing the critical exponents in different phases and plotting the order parameter histograms at the critical point, but due to the limited numerical accuracy, these results could only offer indirect evidence of the existence of emergent continuous symmetries at DQCP. The conserved Noether current that is directly associated with the existence of continuous symmetry has not been tested till now.

Recently, Dr. MA Nvsen and Prof. MENG Ziyang from the Institute of Physics (IOP), Chinese Academy of Sciences (CAS) and assistant Prof. YOU Yizhuang from the University of California at San Diego investigated the emergent symmetry at DQCP on the two dimensional easy-plane JQ model (shown in Figure 1), inspired by the power and conciseness of the Noether’s theorem [5].

The theorem states that every continuous symmetry of a physical system is associated with a corresponding conservation law. The conservation law further manifests itself in the form of a conserved current. Likewise, the observation of a conserved current in a physical system is the direct evidence of the existence of the associated continuous symmetry. These researchers constructed the currents operators in the field theoretical description of the DQCP with emergent O(4) symmetry and found their corresponding operators in the lattice model realization, as shown in the Table 1. Among all the current operators, they found that $J_{23}^0$ – the spin operator $S_x$ at momenta $(\pi, 0)$ – is the most important one in testing the emergent O(4) symmetry in this microscopic system.

With such understanding, these researchers performed large-scale quantum Monte Carlo simulations on the model to test their ideas. They measured the dynamical spin correlation functions at the corresponding momenta, and found that the scaling dimension of $J_{23}^0$ is indeed converged to the integers only related with the space-time dimension of the problem with no renomalization corrections – the unique property of conserved current.
operator. They also tested another conserved current $J^{34}$ using the same method, which is the $S_z$ correlation at momenta (0,0). The simulation results in Figure 2 show that the correction of the scaling dimension $\eta$ of both currents indeed extrapolated to zero at the infinite size limit, which presents a direct evidence for the emergent $O(4)$ symmetry.

The idea of employing a conserved current to detect the emergent continuous symmetry is generic, and the work $^{(5)}$ has already inspired another recent work in a one-dimensional spin system with emergent continuous symmetry $^{(6)}$.


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Contact Institute of Physics, CAS Dr. MENG Ziyang zymeng@iphy.ac.cn Web: http://ziyangmeng.iphy.ac.cn

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